

**AS Level Mathematics B (MEI)**  
**H630/01 Pure Mathematics and**  
**Mechanics**

**Question Set 1**

1. Write  $\frac{8}{3-\sqrt{5}}$  in the form  $a + b\sqrt{5}$ , where  $a$  and  $b$  are integers to be found. **(2)**
2. Find the binomial expansion of  $(3 - 2x)^3$ . **(4)**
- 3.
- (i) Sketch the graphs of  $y = 4\cos(x)$  and  $y = 2\sin(x)$  for  $0^\circ \leq x \leq 180^\circ$  on the same axes. **(2)**
- (ii) Find the exact coordinates of the point of intersection of these graphs, giving your answer in the form  $(\arctan(a), k\sqrt{b})$ , where  $a$  and  $b$  are integers and  $k$  is rational. **(4)**
- (iii) A student argues that without the condition  $0^\circ \leq x \leq 180^\circ$  all the points of intersection of the graphs would occur in the intervals of  $360^\circ$  because both  $\sin(x)$  and  $\cos(x)$  are periodic functions with this period. Comment on the validity of the student's argument. **(1)**

**In this question you must show detailed reasoning.**

4. You are given that  $f(x) = 4x^3 - 3x + 1$ .
- (i) Use the factor theorem to show that  $(x + 1)$  is a factor of  $f(x)$ . **(2)**
- (ii) Solve the equation  $f(x) = 0$ . **(3)**

In this question you must show detailed reasoning.

5. Fig. 5 shows the graph of a quadratic function. The graph crosses the axes at the points  $(-1, 0)$ ,  $(0, -4)$  and  $(2, 0)$ .

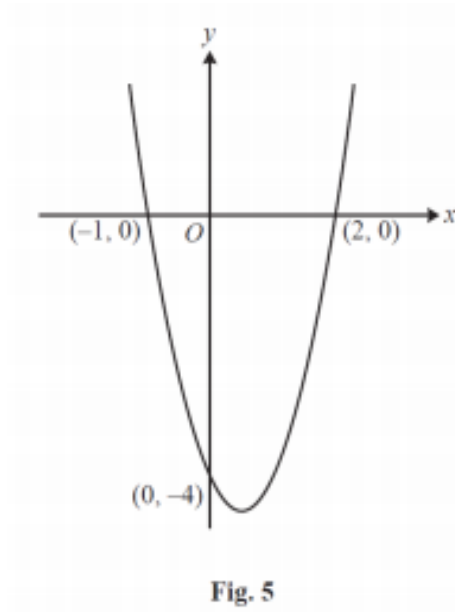


Fig. 5

Find the area of the finite region bounded by the curve and the  $x$ -axis.

**(8)**